

# Package ‘ConsRankClass’

July 21, 2025

**Type** Package

**Title** Classification and Clustering of Preference Rankings

**Version** 1.0.2

**Date** 2025-04-15

**Maintainer** Antonio D'Ambrosio <antdambr@unina.it>

**Depends** ConsRank

**Imports** janitor, methods, pracma, rlist, proxy, smacof, gtools

## Description

Tree-based classification and soft-clustering method for preference rankings, with tools for external validation of fuzzy clustering, and Kemeny-equivalent augmented unfolding.

It contains the recursive partitioning algorithm for preference rankings, non-parametric tree-based method for a matrix of preference rankings as a response variable. It contains also the distribution-free soft clustering method for preference rankings, namely the K-median cluster component analysis (CCA).

The package depends on the 'ConsRank' R package.

Options for validate the tree-based method are both test-set procedure and V-fold cross validation.

The package contains the routines to compute the adjusted concordance index (a fuzzy version of the adjusted rand index) and the normalized degree of concordance (the corresponding fuzzy version of the rand index).

The package also contains routines to perform the Kemeny-equivalent augmented unfolding. The mds engine is the function 'sacofSym' from the package 'smacof'.

Essential references:

D'Ambrosio, A., Vera, J.F., and Heiser, W.J. (2021) <doi:10.1080/00273171.2021.1899892>;

D'Ambrosio, A., Amodio, S., Iorio, C., Pandolfo, G., and Siciliano, R. (2021) <doi:10.1007/s00357-020-09367-0>;

D'Ambrosio, A., and Heiser, W.J. (2019) <doi:10.1007/s41237-018-0069-5>;

D'Ambrosio, A., and Heiser W.J. (2016) <doi:10.1007/s11336-016-9505-1>;

Hullermeier, E., Rifqi, M., Henz-

gen, S., and Senge, R. (2012) <doi:10.1109/TFUZZ.2011.2179303>;

Marden, J.J. <ISBN:0412995212>.

**License** GPL-3

**Encoding** UTF-8

**URL** <https://www.r-project.org/>

**Repository** CRAN

**RoxygenNote** 7.3.2

**NeedsCompilation** no

**Author** Antonio D'Ambrosio [aut, cre]

**Date/Publication** 2025-04-17 07:40:09 UTC

## Contents

augmatrix . . . . .	2
cca . . . . .	4
ccacontrol . . . . .	5
EVS . . . . .	7
fuzzyconcordance . . . . .	8
getsubtree . . . . .	11
Irish . . . . .	12
kunfolding . . . . .	13
layouttree . . . . .	14
mdscontrol . . . . .	15
nodepath . . . . .	16
plot.kunfolding . . . . .	17
plot.ranktree . . . . .	18
predict.ranktree . . . . .	19
print.cca . . . . .	21
print.kunfolding . . . . .	21
print.ranktree . . . . .	22
ranktree . . . . .	22
ranktreecontrol . . . . .	25
summary.cca . . . . .	27
summary.kunfolding . . . . .	27
summary.ranktree . . . . .	28
treepaths . . . . .	28
Univranks . . . . .	29
validatetree . . . . .	31
vecTaux . . . . .	32
<b>Index</b>	<b>34</b>

---

augmatrix

*Kemeny-equivalent augmented dissimilarity matrix*

---

## Description

Kemeny-equivalent augmented dissimilarity matrix

**Usage**

```
augmatrix(X)
```

**Arguments**

**X** A  $n$  by  $m$  data matrix, in which there are  $n$  judges and  $m$  objects to be judged. Each row is a ranking of the objects which are represented by the columns.

**Details**

First the matrix is transformed with the tau\_X rank correlation coefficient, then it is normalized. The output contains:

Delta		the augmented dissimilarity matrix
Interaction		the submatrix containig the interactions individuals-items
Objects		the submatrix containing the within-items proximities
Indiv		the submatrix containing the within-individuals proximities
beta		the beta parameter
alpha		the alpha parameter
csi		the csi parameter
res		the resume of th eaugmentation in terms of:
	TauX	tau_x rank correlation coefficient
	Kendall	kendall rank correlation coefficient
	Spearman	Spearman correlation coefficient

**Value**

A list containing the dissimilarity matrix and othe information about the augmented matrix. See details for detailed information.

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**References**

D'Ambrosio, A., Vera, J. F., & Heiser, W. J. (2022). Avoiding degeneracies in ordinal unfolding using Kemeny-equivalent dissimilarities for two-way two-mode preference rank data. *Multivariate Behavioral Research*, 57(4), 679-699.

cca

*K-Median Cluster Component Analysis***Description**

K-Median Cluster Component Analysis, a distribution-free soft-clustering method for preference rankings.

**Usage**

```
cca(X, k, control = ccacontrol(...), ...)
```

**Arguments**

X	A n by m data matrix containing preference rankings, in which there are n judges and m objects to be judged. Each row is a ranking of the objects which are represented by the columns.
k	The number of cluster components
control	a list of options that control details of the cca algorithm governed by the function ccacontrol. The options govern maximum number of iterations of cca (itercca=1 is the default), the algorithm chosen to compute the median ranking (default, "quick"), and other options related to the consrank algorithm, which is called by cca
...	arguments passed bypassing ccacontrol

**Details**

The user can use any algorithm implemented in the consrank function from the **ConsRank** package. All algorithms allow the user to set the option 'full=TRUE' if the median ranking(s) must be searched in the restricted space of permutations instead of in the unconstrained universe of rankings of n items including all possible ties. There are two classification uncertainty measures: Us and Uprods. "Us" is the geometric mean of the membership probabilities of each individual, normalized in such a way that in the case of maximum uncertainty Us=1. "Ucca" is the average of all the "Us". "Uprods" is the product of the membership probabilities of each individual, normalized in such a way that in the case of maximum uncertainty Uprods=1. "Uprodscca" is the average of all the "Uprods".

**Value**

An object of the class "cca". It contains:

pk	the membership probability matrix
clc	cluster centers
oclc	cluster centers in terms of orderings
idc	crisp partition: id of the cluster component associated with the highest membership probability
Hcca	Global homogeneity measure (tau_X rank correlation coefficient)

hk	Homogeneity within cluster
props	estimated proportion of cases within cluster
Us	Uncertainty measure per-individual (see details)
Ucca	Global uncertainty measure
Uprods	Uncertainty measure per-individual (see details)
Uprodscca	Global uncertainty measure
consrankout	complete output of rank aggregation algorithm, containing eventually multiple median rankings

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**References**

D'Ambrosio, A. and Heiser, W.J. (2019). A Distribution-free Soft Clustering Method for Preference Rankings. *Behaviormetrika*, vol. 46(2), pp. 333–351, DOI: 10.1007/s41237-018-0069-5

Heiser W.J., and D'Ambrosio A. (2013). Clustering and Prediction of Rankings within a Kemeny Distance Framework. In Berthold, L., Van den Poel, D, Ultsch, A. (eds). *Algorithms from and for Nature and Life*.pp-19-31. Springer international. DOI: 10.1007/978-3-319-00035-0\_2.

Ben-Israel, A., and Iyigun, C. (2008). Probabilistic d-clustering. *Journal of Classification*, 25(1), pp.5-26. DOI: 10.1007/s00357-008-9002-z

**See Also**

ccacontrol  
ranktree

**Examples**

```
data(Irish)
set.seed(135) #for reproducibility
# CCA with four components
c cares <- cca(Irish$rankings, 4, itercca=10)
summary(c cares)
```

---

ccacontrol

*Utility function*


---

**Description**

Utility function to use to set the control arguments of cca

**Usage**

```
ccacontrol(
  algorithm = "quick",
  full = FALSE,
  itercca = 1,
  consrankitermax = 10,
  np = 15,
  gl = 100,
  ff = 0.4,
  cr = 0.9,
  proc = FALSE,
  ps = FALSE
)
```

**Arguments**

algorithm	The algorithm used to compute the median ranking. One among "BB", "quick" (default), "fast" and "decor"
full	Specifies if the median ranking must be searched in the universe of rankings including all the possible ties. Default: FALSE
itercca	Number of iterations of cca
consrankitermax	Number of iterations for "fast" and "decor" algorithms. itermax=10 is the default option.
np	(for "decor" only) the number of population individuals. np=15 is the default option.
gl	(for "decor" only) generations limit, maximum number of consecutive generations without improvement. gl=100 is the default option.
ff	(for "decor" only) the scaling rate for mutation. Must be in [0,1]. ff=0.4 is the default option.
cr	(for "decor" only) the crossover range. Must be in [0,1]. cr=0.9 is the default option.
proc	(for "BB" only) proc=TRUE allows the branch and bound algorithm to work in difficult cases, i.e. when the number of objects is larger than 15 or 25. proc=FALSE is the default option
ps	If PS=TRUE, on the screen some information about how many branches are processed are displayed. Default value: FALSE

**Value**

A list containing all the control parameters

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**[cca](#)

---

**EVS***European Values Studies (EVS) data*

---

**Description**

Random sub-sample of 3584 cases of the survey conducted in 1999 in 32 countries analyzed by Vermunt (2003).

**Usage**

```
data("EVS")
```

**Format**

The format is: List of 3

\$ data:'data.frame': 1911 obs. of 11 variables:

country, gender ,yearbird, mstatus (marital status), eduage (age of education completion), employment (Employment status: ordinal scale 1-8), householdinc (Household income: ordinal scale 1-10), A (Maintain order in Nation), Give people more say in Government decisions, (C) Fight rising prices, (D) Protect freedom of speech.

\$ predictors:'data.frame' with all the predictors

\$ rankings : matrix with the preferences for "A" (Maintain order in Nation), "B" (Give people more say in Government decisions), "C" (Fight rising prices), "D" (Protect freedom of speech).

**Details**

Rankings were obtained by applying the post-materialism scale developed by Inglehart (1977). The scale is based upon an experiment of the type "pick 2 out of 4" most important political goals for your Governments. For this reason, replace the 'NA's with 3 before using the rankings with codes 'ranktree' or 'cca' (see D'Ambrosio and Heiser, 2016). About the predictors, the coding of the Countries are: G1 (Austria, Denmark, Netherlands, Sweden), G2 (Belgium, Croatia, France, Greece, Ireland, Northern Ireland, Spain), G3 (Bulgaria, Czechnia, East, Germany, Finland, Iceland, Luxembourg, Malta, Portugal, Romania, Slovenia, West Germany), G4 (Belarus, Estonia, Hungary, Latvia, Lithuania, Poland, Russia, Slovakia, Ukraine). Coding of predictor "mstatus" are: mar (married), wid (widowed), div (divorced), sep (separated), nev (never married).

**Source**

[http://statisticalinnovations.com/technicalsupport/choice\\_datasets.html](http://statisticalinnovations.com/technicalsupport/choice_datasets.html)

## References

- Vermunt, J. K. (2003). Multilevel latent class models. *Sociological Methodology*, 33(1), 213–239.
- Inglehart, R. (1977). *The silent revolution: Changing values and political styles among Western Publics*. Princeton, NJ: Princeton University Press.
- D’Ambrosio, A., and Heiser W.J. (2016). A recursive partitioning method for the prediction of preference rankings based upon Kemeny distances. *Psychometrika*, vol. 81 (3), pp.774-94.

## Examples

```
data(EVS)

# EVS$rankings[is.na(EVS$rankings)] <- 3 #place unranked objects in a tie to the third position
# ccares <- cca(EVS$rankings,4) #solution with 4 components
```

---

fuzzyconcordance	<i>Normalized Degree of Concordance (NDC) and Adjusted Concordance Index (ACI)</i>
------------------	--

---

## Description

Given two fuzzy (Ruspini) partitions, it compute the NDC and the ACI. NDC is the fuzzy version of the Rand Index, as well as ACI is the fuzzy version of the Adjusted Rand Index

## Usage

```
fuzzyconcordance(P, Q, nperms = 1000)
```

## Arguments

- |        |  |
|--------|--|
| P      | A fuzzy partition. It has to be a matrix with n rows and k columns. Each column is expression of the degree of membership of the i-th row over the k partitions (see details). |
| Q      | A fuzzy partition. It has to be a matrix with n rows and h columns. Each column is expression of the degree of membership of the i-th row over the h partitions (see details). |
| nperms | number of permutations necessary to compute ACI. Default: 1000   |

## Details

Both P and Q, or only one of those, can be crisp (or hard) partitions. In this case, each row must contain either 0 or 1, and the sum of the i-th row must be 1. In other words, either P or Q (or both) are expressed in terms of dummy coding. If both partitions are crisp, then NDC is equal to Rand Index and ACI is equal to Adjusted Rand Index. This function can be used to externally validate the output of any fuzzy clustering method



**Value**

A list containing:

ACI	the Adjusted Concordance Index
NDC	the Normalized Degree of Concordance

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**References**

D'Ambrosio, A., Amodio, S., Iorio, C., Pandolfo, G. and Siciliano, R. (2021). Adjusted Concordance Index: an Extension of the Adjusted Rand Index to Fuzzy Partitions. *Journal of Classification* vol. 38(1), pp. 112–128 (2021). DOI: 10.1007/s00357-020-09367-0

Hullermeier, E., Rifqi, M., Henzgen, S., and Senge, R. (2012). Comparing fuzzy partitions: a generalization of the Rand index and related measures. *IEEE Transactions on Fuzzy Systems*, 20(3), 546–556. DOI: 10.1109/TFUZZ.2011.2179303

**See Also**

[cca](#)

**Examples**

```
#two random fuzzy partitions
P = rbind(c(0.5259, 0.1656, 0.3085),
c(0.5623, 0.1036, 0.3341),
c(0.2508, 0.1849, 0.5643),
c(0.5654, 0.1934, 0.2413),
c(0.4529, 0.1679, 0.3792),
c(0.2390, 0.1758, 0.5852),
c(0.3114, 0.1743, 0.5143),
c(0.4188, 0.1392, 0.4420),
c(0.5830, 0.1655, 0.2514),
c(0.5860, 0.1171, 0.2969),
c(0.2630, 0.1706, 0.5664),
c(0.5882, 0.1032, 0.3086),
c(0.5829, 0.1277, 0.2894),
c(0.3942, 0.1046, 0.5012),
c(0.5201, 0.1097, 0.3702),
c(0.2568, 0.1823, 0.5609),
c(0.3687, 0.1695, 0.4618),
c(0.5663, 0.1317, 0.3020),
c(0.5169, 0.1950, 0.2881),
c(0.5838, 0.1034, 0.3128))

Q = rbind(c(0.4494, 0.3755, 0.1751),
c(0.5219, 0.3526, 0.1255),
c(0.3432, 0.5062, 0.1506),
c(0.3120, 0.5181, 0.1699),
```

```

c(0.5362, 0.2747, 0.1891),
c(0.4082, 0.3959, 0.1959),
c(0.4670, 0.3782, 0.1547),
c(0.4276, 0.4585, 0.1139),
c(0.4013, 0.4837, 0.1149),
c(0.3724, 0.5019, 0.1258),
c(0.5055, 0.3104, 0.1841),
c(0.4027, 0.4719, 0.1254),
c(0.3565, 0.4620, 0.1814),
c(0.6106, 0.2650, 0.1244),
c(0.5595, 0.2476, 0.1929),
c(0.4657, 0.3993, 0.1350),
c(0.2964, 0.5839, 0.1197),
c(0.5387, 0.3362, 0.1251),
c(0.4043, 0.4341, 0.1616),
c(0.5631, 0.2895, 0.1473))

ci <- fuzzyconcordance(P,Q)

#generate a random fuzzy partition with two components (clusters)
Q2 <- matrix(runif(20),ncol=1)
Q2 <- cbind(Q2,1-Q2)

ci2 <- fuzzyconcordance(P,Q2)

#generate a random crisp partition
P2 <- t(rmultinom(20,1,c(0.3,0.3,0.4)))

ci3 <- fuzzyconcordance(P2,Q)
#-----
## Not run:
# install.packages("Rankcluster")
library("Rankcluster") # model-based clustering algorithm for
                        # ranking data by Biernacki and Jacques (2013)
                        # <doi:10.1016/j.csda.2012.08.008>

data(APA)
set.seed(136) #for reproducibility
rcres <- rankclust(APA$data,K=3) # solution with 3 centers, it takes about 75 seconds
##
ccares <- cca(APA$data,k=3) #solution with 3 components, it takes about 7 seconds
##
ci <- fuzzyconcordance(rcres[3]@tik,ccares$pk)
ci$ACI # 0.0226 means that the two partitions are similar (see NDC below),
        # but their similarity is mainly due to chance
ci$NDC

## End(Not run)

```

---

`getsubtree`*Determine a tree from the main tree-based structure*

---

**Description**

Given a tree belonging to the class "ranktree", determine a subtree with a given number of terminal nodes

**Usage**

```
getsubtree(Tree, cut, tokeep = NULL)
```

**Arguments**

Tree	An object of the class "ranktree" coming from the function ranktree
cut	The maximum number of terminal nodes that the Tree must have
tokeep	parameter invoked by other internal functions

**Details**

If the pruning sequence returns a series of subtrees with, say, 1,2,4,7,9 terminal nodes and the user set cut=8, the function extract the subtree with 7 terminal nodes.

**Value**

An object of the class "ranktree", containing the same information of the output of the function ranktree

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**Examples**

```
data("Univranks")
tree <- ranktree(Univranks$rankings,Univranks$predictors,num=50)
#see how many terminal nodes have the trees composing the nested sequence of subtrees
infoprun <- tree$pruneinfo$termnodes
#select the tree with, say, 6 terminal nodes
tree6 <- getsubtree(tree,6)
```

Irish

*Irish Election data set***Description**

An opinion poll conducted by Irish Marketing Surveys one month prior to the election in 1997. Interviews were conducted on about 1100 respondents, drawn from 100 sampling areas. Interviews took place at randomly located homes, with respondents selected according to a socioeconomic quota. A range of sociological questions was asked of each respondent, as was their voting preference, if any, for each of the candidates.

**Usage**

```
data("Irish")
```

**Format**

The format is: List of 3

\$ IrishElection: 'data.frame': 1083 obs. of 11 variables: Gender (male, housewife, nonhousewife), marital status (single, married, separated), age, socialclass (five unordered categories), Area (rural, city, town), government satisfaction (no opinion, m satisfied, dissatisfied), Bano, Roch, McAl, Nall, Scal

\$ predictors: 'data.frame' with all the predictors

\$ rankings: matrix with the preferences for "Bano" "Roch" "McAl" "Nall"

**Details**

In the original version of the data, the ranking matrix contains NAs. Here, NAs are replaced with the number 7, to indicate that all the non-stated preferences are in a tie at the last position (see D'Ambrosio and Heiser, 2016). For details about the data set see Gormley and Murphy, 2008.

**Source**

<https://projecteuclid.org/journals/annals-of-applied-statistics/volume-2/issue-4/A-mixture-of-experts-model-for-rank-data-with/10.1214/08-AOAS178.full?tab=ArticleLinkSupplemental>

**References**

Gormley, I.C., and Murphy, T.B. (2008). A mixture of experts model for rank data with applications in election studies. *Annals of Applied Statistics* 2(4): 1452-1477. DOI: 10.1214/08-AOAS178

D'Ambrosio, A., and Heiser W.J. (2016). A recursive partitioning method for the prediction of preference rankings based upon Kemeny distances. *Psychometrika*, vol. 81 (3), pp.774-94. DOI: 10.1007/s11336-016-9505-1.

**Examples**

```
data(Irish)
```

---

 kunfolding

*Kemeny-equivalent augmented unfolding*


---

## Description

Kemeny-equivalent augmented unfolding.

## Usage

```
kunfolding(X, p = 2, control = mdscontrol(...), ...)
```

## Arguments

X	A n by m data matrix, in which there are n judges and m objects to be judged. Each row is a ranking of the objects which are represented by the columns.
p	the dimensionality of the solution. Default p=2
control	a list of options that control details of the kunfolding model governed by the function mdscontrol. The options govern the MDS model ("ordinal" or "metric"), the initial configuration ("torgerson", "random" or "user"), the transformation ("primary", "secondary", "tertiary", "spline", "ratio", "interval", "none"), the set of weights, and other related options
...	arguments passed bypassing mdscontrol

## Details

The MDS engine is smacofsym from smacof. In a future release other mds algorithms will be implemented. The output consists in a object of the class "kunfolding". It contains:

rawstress	raw stress
nrawstress	normalized raw stress
stress1	Stress-1
rowcoord	row (individuals) coordinates
colcord	column (items) coordinates
dhat	dhat
dij	configuration distance
shepardD	DeSarbo I Index
kendallfit	Kendall tau_b between transformed and fitted proximities
tauxfit	Tau_X between transformed and fitted proximities
avgrecov	Averaged recovery measure between raw preference data and fitted proximities
avgedpearson	Averaged Pearson correlation between raw preference data and fitted proximities
avgspearman	Averaged Spearman rho between raw preference data and fitted proximities
avgkendall	Averaged Kendall taub between raw preference data and fitted proximities
avgtaux	Averaged Tau_X between raw preference data and fitted proximities
resume	Resume measures
resumerec	tab Resume of recovery measures
resumeaug	Resume of augmentation matrix

kDelta	Kemeny equivalent dissimilarity matrix
beta	beta parameter
alpha	alpha parameter
interactions	n x m interaction submatrix
csi	csi parameter
mdssol	mds solution as returned by smacof package
n_i	number of individuals
n_c	number of items
tots	total
model	mds model
transf	transformation used

**Value**

An object of the class `kunfolding`. See details for detailed information.

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**References**

D'Ambrosio, A., Vera, J. F., & Heiser, W. J. (2022). Avoiding degeneracies in ordinal unfolding using Kemeny-equivalent dissimilarities for two-way two-mode preference rank data. *Multivariate Behavioral Research*, 57(4), 679-699.

**See Also**

`augmatrix`

**Examples**

```
data("breakfast", package="smacof")
unfout <- kunfolding(breakfast)
itemsl <- colnames(breakfast)
plot(unfout, labs=itemsl)
```

---

layouttree

*Utility function*

---

**Description**

A utility function completing the output of the function `ranktree`.

**Usage**

```
layouttree(Tree)
```

**Arguments**

Tree                    an object of the class "ranktree"

**Value**

an object of the class "ranktree" completing the output of the function ranktree

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

---

mdscontrol                    *Utility function*

---

**Description**

Utility function to use to set the control arguments of kunfolding

**Usage**

```
mdscontrol(
  model = "ordinal",
  init = "torgerson",
  transf = "primary",
  userinit = NULL,
  w = NULL,
  minstress = 1e-05,
  itermax = 500,
  printscr = TRUE,
  spline.degree = 2,
  spline.intKnots = 2,
  relax = FALSE,
  modulus = 1
)
```

**Arguments**

model	Specifies MDS model. One among "ordnal (default)" or "metric"
init	Initial configuration. One among "torgerson" (degault), "random" or "user"
transf	The transformation. One among "primary" (default), "secondary", "tertiary", "spline", "ratio", "interval", "no
userinit	The user initial configuration if "init" has been set as "user"
w	The set of weigths. Default: NULL
minstress	the minimum stress (for stress method). Default 1e-5
itermax	Maximum number if iterations. Default 500
printscr	Display the summary of the model. Default TRUE

spline.degree Degree of spline transformation. Default 2  
spline.intKnots Interior knots. default 2  
relax Relax the solution. Default FALSE  
modulus Modulus. Default 1

**Value**

A list containing all the control parameters

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[kunfolding](#)

---

nodepath *Path of a terminal node*

---

**Description**

Given an object of the class "ranktree", it visualize the path leading to the terminal node

**Usage**

```
nodepath(termnode, Tree)
```

**Arguments**

termnode The terminal node of which the path has to be extracted  
Tree An object of the class "ranktree"

**Value**

The path leading to the terminal node

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[ranktree](#), [treepaths](#), [getsubtree](#)



**Examples**

```

data(Irish)
#build the tree with default options
tree <- ranktree(Irish$rankings,Irish$predictors)
#get information about all the paths leading to terminal nodes
paths <- treepaths(tree)
#see the path for terminal node number 8
nodepath(termnode=8,tree)

```

---

plot.kunfolding                      *Plot Kemeny equivalent augmented unfolding solution*

---

**Description**

Plot the Kemeny equivalent augmented unfolding coming from kunfolding

**Usage**

```

## S3 method for class 'kunfolding'
plot(
  x,
  labs = NULL,
  labsrow = NULL,
  main = NULL,
  cols = NULL,
  cexind = 1,
  cexitems = 1,
  pchcol = 15,
  ...
)

```

**Arguments**

x	An object of the class "kunfolding"
labs	The labels of the items. Defalut is NULL. If not provided, a sequence "o1,...,on" is printed, with n=number of items
labsrow	The labels of the individuals. Defalut is NULL. If not provided, a sequence "1,...,m" is printed, with m=number of individuals
main	Main title of the plot. Default NULL
cols	Color of the individuals. It must be numeric. Default is NULL (dark gray).
cexind	cex of the individuals. Default 1
cexitems	cex of the items. defaul 1
pchcol	pch parameter for items points. Default 15
...	System reserved (No specific usage)

**Value**

the plot of unfolding solution

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[kunfolding](#), [augmatrix](#)

**Examples**

```
data("breakfast", package="smacof")
unfout <- kunfolding(breakfast)
itemsl <- colnames(breakfast)
plot(unfout, labs=itemsl, cexitems=0.8)
```

---

plot.ranktree

*Plot tree-based structure or pruning sequence of ranktree*

---

**Description**

Plot the tree coming from the ranktree or the pruning sequence of the ranktree

**Usage**

```
## S3 method for class 'ranktree'
plot(
  x,
  plot.type = "tree",
  dispclass = FALSE,
  valtree = NULL,
  taos = TRUE,
  ...
)
```

**Arguments**

x	An object of the class "ranktree"
plot.type	One among "tree" or "pruningseq"
dispclass	Display the median ranking above terminal nodes. Default option: FALSE
valtree	If plot.type="pruningseq", it shows the Tau_x rank correlation coefficient or the error along the pruning sequence on the training set. If valtree is the output of the function <code>validatetree</code> , it shows either the Tau_x rank correlation coefficient or the error along the pruning sequence of also the decision tree (validated by wither test set or cross-validation)

taos	If plot.type="pruningseq", it plots the Tau_x rank correlation coefficient along the pruning sequence. If taos=FALSE, it plots the error.
...	System reserved (No specific usage)

**Value**

the plot of either the tree or the pruning sequence

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[ranktree](#), [validatetree](#)

**Examples**

```
data("Univranks")
tree <- ranktree(Univranks$rankings,Univranks$predictors,num=50)
plot(tree,dispclass=TRUE)

data(EVS)
EVS$rankings[is.na(EVS$rankings)] <- 3
set.seed(654)
training=sample(1911,1434)
tree <- ranktree(EVS$rankings[training,],EVS$predictors[training,],decrmin=0.001,num=50)
plot(tree,dispclass=TRUE)
#test set validation
vtreetest <- validatetree(tree,testX=EVS$predictors[-training,],EVS$rankings[-training,])
dtree <- getsubtree(tree,vtreetest$best_tau)
plot(dtree,dispclass=TRUE)
#see the global weighted tau_X rank correlation coefficients
plot(tree,plot.type="pruningseq",valtree=vtreetest)
#see the error rates
plot(tree,plot.type="pruningseq",valtree=vtreetest, taos=FALSE)
```

---

predict.ranktree

*Predict the median rankings for new observations*

---

**Description**

Predict the median rankings in a tree-based structure built with ranktree for new observations

**Usage**

```
## S3 method for class 'ranktree'
predict(object, newx, ...)
```

**Arguments**

object	An object of the class "ranktree"
newx	A dataframe of the same nature of the predictor dataframe with which the tree has been built
...	System reserved (No specific usage)

**Value**

A list containing:

rankings	the fit in terms of rankings
orderings	the fit in terms of orderings
info	dataframe containing the terminal nodes in which the new x fall down, then the new x and the fit (in terms of rankings)

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[ranktree](#) [validatetree](#)

**Examples**

```
data(EVS)
EVS$rankings[is.na(EVS$rankings)] <- 3
set.seed(654)
training=sample(1911,1434)
tree <- ranktree(EVS$rankings[training,],EVS$predictors[training,],decrmin=0.001,num=50)
#use the function predict to predict rankings for new predictors
rankfit <- predict(tree,newx=EVS$predictors[-training,])
#fit in terms of rankings
rankfit$rankings
#fit in terms of orderings
rankfit$orderings
# information about the fit (terminal node, predictor and fit (in terms of rankings))
rankfit$info
```

---

print.cca	<i>S3 methods for cca</i>
-----------	---------------------------

---

**Description**

Print methods for objects of class cca

**Usage**

```
## S3 method for class 'cca'  
print(x, ...)
```

**Arguments**

x	An object of the class "cca"
...	not used

**Value**

print a brief summary of the CCA

---

print.kunfolding	<i>S3 methods for kunfolding</i>
------------------	----------------------------------

---

**Description**

Print methods for objects of class kunfolding

**Usage**

```
## S3 method for class 'kunfolding'  
print(x, ...)
```

**Arguments**

x	An object of the class "kunfolding"
...	not used

**Value**

print a brief summary of the Kemeny equivalent augmented unfolding

---

```
print.ranktree      S3 methods for ranktree
```

---

**Description**

Print methods for objects of class ranktree

**Usage**

```
## S3 method for class 'ranktree'
print(x, ...)
```

**Arguments**

x	An object of the class "ranktree"
...	not used

**Value**

print a brief summary of the prediction tree

**Examples**

```
data("Univranks")
tree <- ranktree(Univranks$rankings,Univranks$predictors,num=50)
tree
```

---

```
ranktree      Recursive partitioning method for the prediction of preference rankings based upon Kemeny distances
```

---

**Description**

Recursive partitioning method for the prediction of preference rankings based upon Kemeny distances.

**Usage**

```
ranktree(Y, X, prunplot = FALSE, control = ranktreecontrol(...), ...)
```

**Arguments**

Y	A n by m data matrix, in which there are n judges and m objects to be judged. Each row is a ranking of the objects which are represented by the columns.
X	A dataframe containing the predictor, that must have n rows.
prunplot	prunplot=TRUE returns the plot of the pruning sequence. Default value: FALSE
control	a list of options that control details of the ranktree algorithm governed by the function ranktreecontrol. The options govern the minimum size within node to split (the default value is 0.1*n, where n is the total sample size), the bound on the decrease in impurity, (default, 0.01), the algorithm chosen to compute the median ranking (default, "quick"), and other options related to the consrank algorithm, which is called by ranktree
...	arguments passed bypassing ranktreecontrol

**Details**

The user can use any algorithm implemented in the consrank function from the **ConsRank** package. All algorithms allow the user to set the option 'full=TRUE' if the median ranking(s) must be searched in the restricted space of permutations instead of in the unconstrained universe of rankings of n items including all possible ties. The output consists in a object of the class "ranktree". It contains:

X	the predictors: it must be a dataframe
Y	the response variable: the matrix of the rankings
node	a list containing teh tree-based structure:
number	node number
terminal	logical: TRUE is terminal node
father	father node number of the current node
idfather	id of the father node of the current node
size	sample size within node
impur	impurity at node
wimpur	weighted impurity at node
idatnode	id of the observations within node
class	median ranking within node in terms of orderings
nclass	median ranking within node in terms of rankings
mclass	eventual multiple median rankings
tau	Tau_x rank correlation coefficient at node
wtau	weighted Tau_x rank correlation coefficient at node
error	error at node
werror	weighted error at node
varsplit	variables generating split
varsplitid	id of variables generating split
cutspli	splitting point
children	children nodes generated by current node
idchildren	id of children nodes generated by current node
...	other info about node
control	parameters used to build the tree
numnodes	number of nodes of the tree

tsynt		list containing the synthesis of the tree:
	children	list containing all information about leaves
	parents	list containing all information about parent nodes
geneaoly		data frame containing information about all nodes
idgenealogy		data frame containing information about all nodes in terms of nodes id
idparents		id of the parents of all the nodes
goodness		goodness -and badness- of fit measures of the tree: Tau_X, error, impurity
nomin		information about nature of the predictors
alpha		alpha parameter for pruning sequence
pruneinfo		list containing information about the pruning sequence:
	prunelist	information about the pruning
	tau	tau_X rank correlation coefficient of each subtree
	error	error of each subtree
	termnodes	number of terminal nodes of each subtree
subtrees		list of each subtree created with the cost-complexity pruning procedure

**Value**

An object of the class ranktree. See details for detailed information.

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**References**

D'Ambrosio, A., and Heiser W.J. (2016). A recursive partitioning method for the prediction of preference rankings based upon Kemeny distances. *Psychometrika*, vol. 81 (3), pp.774-94.

**See Also**

ranktreecontrol, plot.ranktree, summary.ranktree, getsubtree, validatetree, treepaths, nodepath

**Examples**

```
data("Univranks")
tree <- ranktree(Univranks$rankings,Univranks$predictors,num=50)
```

```
data(Irish)
#build the tree with default options
tree <- ranktree(Irish$rankings,Irish$predictors)
```

```
#plot the tree
plot(tree,dispclass=TRUE)
```

```
#visualize information
summary(tree)
```



```
#get information about the paths leading to terminal nodes (all the paths)
infopaths <- treepaths(tree)

#the terminal nodes
infopaths$leaves

#sample size within each terminal node
infopaths$size

#visualize the path of the second leaf (terminal node number 8)
infopaths$paths[[2]]

#alternatively
nodepath(termnode=8,tree)

set.seed(132) #for reproducibility
#validation of the tree via v-fold cross-validation (default value of V=5)
vtree <- validatetree(tree,method="cv")

#extract the "best" tree
dtree <- getsubtree(tree,vtree$best_tau)

summary(dtree)

#plot the validated tree
plot(dtree,dispclass=TRUE)

#predicted rankings
rankfit <- predict(dtree,newx=Irish$predictors)

#fit of rankings
rankfit$rankings

#fit in terms of orderings
rankfit$orderings

#all info about the fit (id og the leaf, predictor values, and fit)
rankfit$orderings
```

---

ranktreecontrol

*Utility function*

---

## Description

Utility function to use to set the control arguments of ranktree

**Usage**

```
ranktreecontrol(
  num = NULL,
  decrmin = 0.01,
  algorithm = "quick",
  full = FALSE,
  itermax = 10,
  np = 15,
  gl = 100,
  ff = 0.4,
  cr = 0.9,
  proc = FALSE,
  ps = FALSE
)
```

**Arguments**

num	The maximum number of observations in a node to be split: default, 10% of the sample size
decrmin	Minimum decrease in impurity
algorithm	The algorithm used to compute the median ranking. One among "BB", "quick" (default), "fast" and "decor"
full	Specifies if the median ranking must be searched in the universe of rankings including all the possible ties. Default: FALSE
itermax	Number of iterations for "fast" and "decor" algorithms. itermax=10 is the default option.
np	(for "decor" only) the number of population individuals. np=15 is the default option.
gl	(for "decor" only) generations limit, maximum number of consecutive generations without improvement. gl=100 is the default option.
ff	(for "decor" only) the scaling rate for mutation. Must be in [0,1]. ff=0.4 is the default option.
cr	(for "decor" only) the crossover range. Must be in [0,1]. cr=0.9 is the default option.
proc	(for "BB" only) proc=TRUE allows the branch and bound algorithm to work in difficult cases, i.e. when the number of objects is larger than 15 or 25. proc=FALSE is the default option
ps	If PS=TRUE, on the screen some information about how many branches are processed are displayed. Default value: FALSE

**Value**

A list containing all the control parameters

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**[ranktree](#)

---

`summary.cca`*S3 methods for ranktree*

---

**Description**

Summary methods for objects of class cca

**Usage**

```
## S3 method for class 'cca'
summary(object, ...)
```

**Arguments**

<code>object</code>	An object of the class "cca"
<code>...</code>	not used

**Value**

it shows the summary of the prediction tree

---

`summary.kunfolding`*S3 methods for kunfolding*

---

**Description**

Summary methods for objects of class kunfolding

**Usage**

```
## S3 method for class 'kunfolding'
summary(object, ...)
```

**Arguments**

<code>object</code>	An object of the class "kunfolding"
<code>...</code>	not used

**Value**

it shows the summary of the Kemeny equivalent augmented unfolding

---

summary.ranktree      *S3 methods for ranktree*

---

**Description**

Summary methods for objects of class ranktree

**Usage**

```
## S3 method for class 'ranktree'  
summary(object, ...)
```

**Arguments**

object	An object of the class "ranktree"
...	not used

**Value**

it shows the summary of the prediction tree

**Examples**

```
data("Univranks")  
tree <- ranktree(Univranks$rankings,Univranks$predictors,num=50)  
summary(tree)
```

---

treepaths      *Path of a terminal node*

---

**Description**

Given an object of the class "ranktree", it extracts the paths of all terminal nodes

**Usage**

```
treepaths(Tree)
```

**Arguments**

Tree	An object of the class "ranktree"
------	-----------------------------------

**Value**

A list containing:

leaves	the number of the terminal nodes
size	the sample size within each terminal nodes
paths	a list containing all the paths

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**See Also**

[ranktree](#), [nodepath](#), [getsubtree](#)

**Examples**

```
data(Irish)
#build the tree with default options
tree <- ranktree(Irish$rankings,Irish$predictors)
#get information about all the paths leading to terminal nodes
paths <- treepaths(tree)
#
#the terminal nodes
paths$leaves
#
#sample size within each terminal node
paths$size
#
#visualize the path of the second leave (terminal node number 8)
paths$paths[[2]]
```

---

Univranks

*University rankings dataset.*

---

**Description**

University rankings dataset was analysed by Dittrich, Hatzinger and Katzenbeisser (1998) to investigate paired comparison data concerning European universities and student's characteristics with the goal to show that university rankings are different for different groups of students. Here both raw data (with paired comparisons) and the version with rankings are presented (see details). A survey of 303 students studying at the Vienna University of Economics was carried out to examine the student's preference of six universities, namely London, Paris, Milan, St. Gallen, Barcelona and Stockholm. The data set contains 23 variables. The first 15 digits in each row indicate the preferences of a student. For a given comparison, responses were coded by 1 if the first preference was preferred, by 2 if the second university was preferred, and by 3 if universities are tied. All rows containing missing ranked Universities were skipped.

**Usage**

```
data("Univranks")
```

**Format**

The format is: List of 3

\$ rawdata: 'data.frame': 212 obs. of 23 variables: the first 15 are the paired comparisons coded as follows: (1: the first is preferred to the second; 2: the second is preferred to the first; 3 tied)

\$ LP : comparison of London to Paris

\$ LM : comparison of London to Milan

\$ PM : comparison of London to Milan

\$ LSg : comparison of London to St. Gallen

\$ PSg : comparison of Paris to St. Gallen

\$ MSg : comparison of Milan to St. Gallen

\$ LB : comparison of London to Barcelona

\$ PB : comparison of Paris to Barcelona

\$ MB : comparison of Milan to Barcelona

\$ SgB : comparison of St. Gallen to Barcelona

\$ LSt : comparison of London to Stockholm

\$ PSt : comparison of Paris to Stockholm

\$ MSt : comparison of Milan to Stockholm

\$ SgSt: comparison of St. Gallen to Stockholm

\$ BSt : comparison of Barcelona to Stockholm

\$ Stud: Factor w/ 2 levels "commerce","other"

\$ Eng : Factor w/ 2 levels "good","poor"

\$ Fra : Factor w/ 2 levels "good","poor"

\$ Spa : Factor w/ 2 levels "good","poor"

\$ Ita : Factor w/ 2 levels "good","poor"

\$ Wor : Factor w/ 2 levels "no","yes"

\$ Deg : Factor w/ 2 levels "no","yes"

\$ Sex : Factor w/ 2 levels "female","male"

\$ predictors:'data.frame': 212 obs. of 8 variables( the last 8 variables of the "rawdata" dataframe

\$ rankings : matrix of preference rankings. The columns are: "L" (London), "P" (Paris), "M" (Milan), "Sg" (St. Gallen), "B" (Barcelona), "St" (Stockholm)

## Details

To obtain the preference rankings from the paired comparisons the procedure has been the following: the first row of the raw data is [1 3 2 1 2 1 1 2 1 1 1 2 1 1 2]. London is preferred to Paris, St. Gallen, Barcelona, Stockholm (LP, LM, LSg, LB and LSt are always equal to 1), and there is no preference between London and Milan (they are tied); Milan is preferred to Paris (PM = 2), St. Gallen, Barcelona and Stockholm; and so on. The first ordering is then  $\langle \{L M\} Sg St B P \rangle$  corresponding to a ranking [1, 5, 1, 2, 4, 3], where the columns indicate L P M Sg B St.

## Source

<http://www.blackwellpublishers.co.uk/rss>

## References

Dittrich, R., Hatzinger, R., and Katzenbeisser, W. (1998). Modelling the effect of subject-specific covariates in paired comparison studies with an application to university rankings. *Journal of the Royal Statistical Society: Series C (Applied Statistics)*, 47(4), 511-525. DOI: 10.1111/1467-9876.00125

D'Ambrosio, A. (2008). Tree based methods for data editing and preference rankings. Ph.D. thesis, University of Naples Federico II. <https://www.doi.org/10.6092/UNINA/FEDOA/2746>

## Examples

```
data(Univranks)
```

---

validatetree

*Validation of the tree for preference rankings*

---

## Description

Validation of the tree either with a test set procedure or with v-fold cross validation

## Usage

```
validatetree(  
  Tree,  
  testX = NULL,  
  testY = NULL,  
  method = "test",  
  V = 5,  
  plotting = TRUE  
)
```

**Arguments**

Tree	An object of the class "ranktree" coming from the function ranktree
testX	The data frame containing the test set (predictors)
testY	The matrix obtaining the test set (response)
method	One between "test" (default) or "cv"
V	The cross-validation parameter. Default V=5
plotting	With the default option plotting=TRUE, the pruning sequence plot is visualized

**Value**

A list containing:

tau	the Tau_x rank correlation coefficient of the sequence of the trees
error	the error of the sequence of the trees
termnodes	the number of terminal nodes of the sequence of the trees
best_tau	the best tree in terms of Tau_x rank correlation coefficient
best_error	the best tree in terms of error (it is the same)
validation	information about the validation procedure

**Author(s)**

Antonio D'Ambrosio <antdambr@unina.it>

**Examples**

```
data(EVS)
EVS$rankings[is.na(EVS$rankings)] <- 3
set.seed(654)
training=sample(1911,1434)
tree <- ranktree(EVS$rankings[training,],EVS$predictors[training,],decrmin=0.001,num=50)
#test set validation
vtreetest <- validate(tree, testX=EVS$predictors[-training,],EVS$rankings[-training,])
#cross-validation
vtreecv <- validate(tree,method="cv",V=10)
```

---

vecTaux

*Tau\_x rank correlation coefficient for vectors*

---

**Description**

Tau\_x rank correlation coefficient for large vectors

**Usage**

```
vecTaux(X, Y)
```



**Arguments**

X	A vector of length n
Y	A vector of length n

**Value**

The tau\_x rank correlation coefficient between the 2 vectors

# Index

- \* **Adjusted**
    - cca, 4
  - \* **Concordance**
    - cca, 4
  - \* **Degree**
    - cca, 4
  - \* **Index**
    - cca, 4
  - \* **Kemeny-equivalent**
    - augmatrix, 2
    - kunfolding, 13
  - \* **Normalized**
    - cca, 4
  - \* **Preference**
    - cca, 4
    - ranktree, 22
  - \* **Recursive**
    - ranktree, 22
  - \* **Soft**
    - cca, 4
  - \* **Tree-based**
    - plot.ranktree, 18
    - ranktree, 22
  - \* **Unfolding**
    - augmatrix, 2
    - kunfolding, 13
    - plot.kunfolding, 17
  - \* **augmented**
    - kunfolding, 13
  - \* **clustering**
    - cca, 4
  - \* **datasets**
    - EVS, 7
    - Irish, 12
    - Univranks, 29
  - \* **dissimilarity**
    - augmatrix, 2
  - \* **method**
    - ranktree, 22
  - \* **of**
    - cca, 4
  - \* **partitioning**
    - ranktree, 22
  - \* **pruning**
    - plot.ranktree, 18
  - \* **rankings**
    - cca, 4
    - ranktree, 22
  - \* **sequence**
    - plot.ranktree, 18
  - \* **structure**
    - plot.ranktree, 18
  - \* **unfolding**
    - kunfolding, 13
- augmatrix, 2, 18
- cca, 4, 7, 9
- ccacontrol, 5
- EVS, 7
- fuzzyconcordance, 8
- getsubtree, 11, 16, 29
- Irish, 12
- kunfolding, 13, 16, 18
- layouttree, 14
- mdscontrol, 15
- nodepath, 16, 29
- plot.kunfolding, 17
- plot.ranktree, 18
- predict.ranktree, 19
- print.cca, 21
- print.kunfolding, 21

print.ranktree, [22](#)

ranktree, [16](#), [19](#), [20](#), [22](#), [27](#), [29](#)

ranktreecontrol, [25](#)

summary.cca, [27](#)

summary.kunfolding, [27](#)

summary.ranktree, [28](#)

treepaths, [16](#), [28](#)

Univranks, [29](#)

validatetree, [19](#), [20](#), [31](#)

vecTaux, [32](#)